

## Equations of Motion, Force, Work, Energy et al

### Equations Motion

For constant acceleration we define

$$a = (v - u) / t$$

and we rearrange to get 1)  $v = u + a t$

(no  $s$  term)

From the concept that distance is average

speed  $\times$  time we get 2)  $s = \frac{1}{2} (u + v) t$

(no  $a$  term)

Putting the value of  $v$  from 1) into 2) we get

$$3) s = u t + \frac{1}{2} a t^2$$

(no  $v$  term)

Putting the value of  $u$  from 1) into 2) we get

$$4) s = v t - \frac{1}{2} a t^2$$

(no  $u$  term)

Finally putting  $t$  from 1) into 2) we get

$$5) v^2 = u^2 + 2 a s$$

(no  $t$  term)

Thus we work with five equations, each equation inter-relating 4 terms from “ $s$   $u$   $v$   $a$   $t$ ” and leaving out the 5<sup>th</sup>. It is recommended the student carries out each of these substitutions to gain familiarity.

nb Differentiating 1) gives the definition of acceleration.

Differentiating 3) gives 1).

### Force, Work, Energy, Momentum Impulse

force = mass  $\times$  acceleration

$$F = m a$$

work = force  $\times$  distance

$$W = F s$$

*Energy is the potential to do work so has the same units*

power = rate of doing work

$$P = F s/t$$

momentum = mass  $\times$  velocity

$$p = m v$$

impulse = force  $\times$  time (duration)

$$I = F \times \Delta t$$

hence impulse = change in momentum

$$I = m v - m u$$

*the units are thus either kg-m/s or N-s*

*In collisions, momentum after = momentum before so*

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

### Moments

If force  $[a \ b]$  acts on position vector  $(x_1, y_1)$  the moment about  $(0,0)$  taking anticlockwise as positive is  $-(y_1 a) + (x_1 b)$

The moment about  $(x_2, y_2)$  is

$$-(y_1 - y_2) a + (x_1 - x_2) b$$

$\otimes$   $rg$